



Department of Electronics and Communication Engineering

MA 8451 – Probability and Random Processes

Unit II - MCQ Bank

1. Let S be the sample space associated with a random experiment E . Let $X=X(S)$ and $Y=Y(S)$ be two functions each assigning a real number to each $s \in S$. Then (X, Y) is called a---

- A. Two Dimensional random Variable
- B. Variance
- C. Mean
- D. Random Variable

Answer: (A)

2. The following table gives the joint probability distribution of X and Y . Find the marginal density functions of X

Y/X	1	2	3
1	0.1	0.1	0.2
2	0.2	0.3	0.1

A.

X	1	2	3
$P(X=x)$	0.3	0.4	0.3

B.

X	1	2	3
$P(X=x)$	0.4	0.4	0.2

C.

X	1	2
$P(X=x)$	0.6	0.4

D.

X	1	2
$P(X=x)$	0.4	0.6

Answer: (A)

3. If $f(x, y) = kxye^{-(x^2+y^2)}$ $x \geq 0, y \geq 0$ is the joint pdf, find k .

- A. 1
- B. 2
- C. 3
- D. 4

Answer: (D)

4. The joint p.m.f of (X,Y) is given by $P(x, y) = k(2x + 3y)$, $x = 0, 1, 2$ $y = 1, 2, 3$. Find the marginal probability distribution of X.

A.

X	0	1	2
P(X=x)	18/72	24/72	30/72

B.

X	1	2	3
P(X=x)	0.4	0.4	0.2

C.

X	1	2
P(X=x)	0.6	0.4

D.

X	1	2
P(X=x)	0.4	0.6

Answer: (A)

5. If X and Y are independent RVs with variances 8 and 5. find the variance of $3X+4Y$

- A. 151
- B. 152
- C. 153
- D. 154

Answer: (B)

6. Find the value of k if $f(x, y) = k(1-x)(1-y)$ for $0 < x, y < 1$ is to be joint density function.

- A. 1
- B. 2
- C. 3
- D. 4

Answer: (D)

7. If X and Y are random variables having the joint p.d.f $f(x, y) = \frac{1}{8}(6-x-y)$, $0 < x < 2$, $2 < y < 4$.

Find $P(X < 1, Y < 3)$.

- A. 3/7
- B. 3/8
- C. 2/8
- D. 4/8

Answer: (B)

8. The Lines of regression in a bivariate distribution are $x+9y=7$ and $y+4x=49/3$. Find the Co-efficient of correlation.

- A. $b_{yx} = -\frac{1}{9}$
- B. $b_{xy} = -\frac{1}{4}$
- C. $b_{yx} = -\frac{2}{9}$ & $b_{xy} = -\frac{3}{4}$
- D. Both (A) & (B)

Answer: (D)

9. The acute angle between the two lines of regression is

- A. $\tan\theta = \left(\frac{1-r^2}{r}\right)\left(\frac{\sigma_x-\sigma_y}{\sigma_x^2+\sigma_y^2}\right)$
- B. $\sin\theta = \left(\frac{1-r^2}{r}\right)\left(\frac{\sigma_x-\sigma_y}{\sigma_x^2+\sigma_y^2}\right)$
- C. $\tan\theta = \left(\frac{1+r^2}{r}\right)\left(\frac{\sigma_x-\sigma_y}{\sigma_x^2+\sigma_y^2}\right)$
- D. $\tan\theta = \left(\frac{1-r^2}{r}\right)\left(\frac{\sigma_x+\sigma_y}{\sigma_x^2+\sigma_y^2}\right)$

Answer: (A)

10. The equation of line of regression of y on x is ---

A. $(y - \bar{y}) = b_{yx}(x - \bar{x})$

B. $(y - \bar{y}) = b_{xy}(x - \bar{x})$

C. $(x - \bar{x}) = b_{xy}(y - \bar{y})$

D. $(x - \bar{x}) = b_{yx}(y - \bar{y})$

Answer: (A)

11. What do you mean by correlation between two random variables?

A. Degree of relationship

B. Nature of relationship

C. Both (A) & (B)

D. None of these

Answer: (C)

12. Let (X,Y) be a two dimensional random variable. Define co-variance of (X,Y).

A. $\text{Cov}(X,Y) = E(XY) - E(X)E(Y)$

B. $\text{Cov}(X,Y) = E(XY) - E(X)$

C. $\text{Cov}(X,Y) = E(XY) - E(Y)$

D. $\text{Cov}(X,Y) = E(X) - E(X)E(Y)$

Answer: (A)

13. Let (X,Y) be a two dimensional random variable. If X and Y are independent. What will be the co-variance of (X,Y).

A. 1

B. 2

C. 3

D. 0

Answer: (D)

14. A measure of association between two random variables obtained as the expected value of the product of the two random variables around their means is called as

- A. Correlation
- B. Auto correlation
- C. Covariance
- D. Auto Covariance

Answer: (C)

15. The regression lines of X on Y and Y on X are $5x-y=22$, $64x-45y=24$ respectively. Find means of X and Y.

- A. $\bar{x} = 6, \bar{y} = 8$
- B. $\bar{x} = 7, \bar{y} = 8$
- C. $\bar{x} = 6, \bar{y} = 9$
- D. $\bar{x} = 7, \bar{y} = 9$

Answer: (A)

16. The minimum and maximum values of the correlation coefficient are --- and ---

- A. 1, -1
- B. 1, 2
- C. 0, 1
- D. -1, 1

Answer: (D)

17. When we say the two random variables are said to be orthogonal?

- A. Their correlation is zero
- B. Their correlation is non-zero
- C. Their correlation is one
- D. None of these

Answer: (A)

18. The Properties of correlation coefficient are

- A. Correlation coefficient does not exceed unity
- B. When $r=1$, the correlation coefficient is perfect and positive
- C. Two independent variables are uncorrelated.
- D. All the above

Answer: (D)

19. The real life example for positive correlation are

- A. The heights and weights of a group of persons, Income and expenditure
- B. Price and demand of a commodity, correlation between volume and pressure of a perfect gas
- C. Both (a) and (b)

Answer: (A)

20. Let X and Y be Continuous Random variable with joint PDF

$$f_{XY}(x, y) = \frac{x(x-y)}{8}, 0 < x < 2 \text{ and } -x < y < x \text{ And } f_{XY}(x, y) = 0 \text{ elsewhere. Find } f_{y/x}(y/x)$$

- A. $\frac{x(x-y)}{2x^3}$
- B. $\frac{x(x+y)}{2x^3}$
- C. $\frac{x(x+y)}{x^3}$
- D. $\frac{x(x-y)}{2x^3}$

Answer: (A)

21. Given the RV X with density function $f(x) = \begin{cases} 2x, & 0 < x < 1 \\ 0, & \text{elsewhere} \end{cases}$ Find PDF of $y = 8x^3$

- A. $\frac{1}{9}y^{-\frac{1}{3}}$
- B. $\frac{1}{6}y^{-\frac{1}{3}}$
- C. $y^{-\frac{1}{3}}$
- D. $\frac{1}{6}y^{-\frac{2}{3}}$

Answer: (B)

22. If two RV deviate in the same direction, then the correlation said to be

- A. Positive
- B. Negative
- C. Neither positive nor negative

Answer: (A)

23. Method of studying Correlation are

- A. Scatter diagram method and Graphical method
- B. Rank method and Concurrent deviation method
- C. Karl Pearson's coefficient of correlation and Method of least squares.
- D. All the above

Answer: (D)

24. The real life example for negative correlation are

- A. The heights and weights of a group of persons, Income and expenditure
- B. Price and demand of a commodity, correlation between volume and pressure of a perfect gas
- C. Both (a) and (b)

Answer: (B)

25. The lifetime of a certain brand of an electric bulb may be considered as a RV with mean 1200h and standard deviation 250h. Find the probability, using central limit theorem, that the average lifetime of 60 bulbs exceeds 1250h.

- A. 6.006
- B. 0.606
- C. 0.0606.
- D. 6.666

Answer: (C)